

Working Problems for BSE 5034 Stochastic Hydrology (2017)

WP-3 Fundamentals of Hydrological Frequency Analysis (HFA-1)

- (1) Conduct a Chi-square GOF test to determine whether the data in Problem 2 of WP-2 can be characterized by (i) a Gumbel distribution and (ii) a normal distribution. [Note: the number of categories = 10.]

Note: By default, the chi square test in R is conducted using equiprobable intervals. However, it can be changed by specifying probabilities of individual intervals.

`chisq.test(x, p = rep(1/length(x), length(x)))`

- (2) Conduct a KS GOF test to determine whether the data in Problem 2 of WP-2 can be characterized by (i) a Gumbel distribution and (ii) a normal distribution.
- (3) The values of $D_{n,\alpha}$ of the KS GOF test is shown in the following table. Based on the asymptotic distribution of $\sqrt{n}[F_n(X) - F_X(X)]$ derived in Problem 3 of WP-2, design and conduct a stochastic (Monte Carlo) simulation to verify the following table.

$$D_{n,\alpha} = \frac{x_{1-\alpha}}{\sqrt{n}}$$

| n | $D_{n,0.05}$ | $D_{n,0.01}$ |
|-----|-----------------|-----------------|
| 15 | 0.338 | 0.404 |
| 16 | 0.328 | 0.392 |
| 17 | 0.318 | 0.381 |
| 18 | 0.309 | 0.371 |
| 19 | 0.301 | 0.363 |
| 20 | 0.294 | 0.356 |
| 25 | 0.27 | 0.32 |
| 30 | 0.24 | 0.29 |
| 35 | 0.23 | 0.27 |
| >35 | $1.36/\sqrt{n}$ | $1.63/\sqrt{n}$ |